MATH 215 Practice

1. What must a transformation T from \mathbf{R}^m to \mathbf{R}^n satisfy in order to be a linear transformation?

2. If $T: \mathbb{R}^2 \to \mathbb{R}^3$ is a linear transformation, such that T([1,0]) = [2,1,3] and T([0,1]) = [1,0,-2], find T([2,3]).

3. Let $T: \mathbb{R}^2 \to \mathbb{R}^3$ be the linear transformation such that $T\left(\begin{bmatrix} 1 \\ 0 \end{bmatrix}\right) = \begin{bmatrix} 1 \\ 4 \\ 0 \end{bmatrix}$ and $T\left(\begin{bmatrix} 0 \\ 1 \end{bmatrix}\right) = \begin{bmatrix} -1 \\ 3 \\ -1 \end{bmatrix}$. Find the standard matrix representation of T.