

This is the MTH 452 HW for sections 6.4 and 6.5\*.  
It is due on Thursday, Feb. 24. Also, we will have a quiz then.  
Orlando M.

### Sec. 6.4:

6.4.4, 6.4.5, 6.4.7, 6.4.8, 6.4.10, 6.4.12, 6.4.18

### Sec. 6.5 (well, not 6.5 from the book but from the notes)

- 6.5.1 Let  $X_1, \dots, X_n$  be a random sample from a normal distribution with  $\sigma^2 = 64$ .
- Show that  $C = \{(x_1, \dots, x_n) : \bar{x} \leq c\}$  is a best critical region for testing  $H_0 : \mu = 80$  against  $H_1 : \mu = 76$ .
  - Find  $n$  and  $c$  so that  $\alpha = 0.05$  and  $\beta = 0.05$  approximately.
- 6.5.2 Let  $X_1, \dots, X_n$  be a random sample of Bernoulli trials with probability of success =  $p$ .
- Show that the best critical region for testing  $H_0 : p = 0.9$  against  $H_1 : p = 0.8$  can be based on the statistic  $Y = \sum_{\ell=1}^n X_\ell$ , which is binomial( $n, p$ ).
  - If  $C = \{(x_1, \dots, x_n) : \sum_{\ell=1}^n x_\ell \leq 0.85n\}$  and  $Y = \sum_{\ell=1}^n X_\ell$ , use the normal approximation to the binomial dist. to find the value of  $n$  such that  $\alpha = 0.10 = P(Y \leq 0.85n ; p = 0.9)$
  - What is the approximate value of  $\beta$  for the test given in part (b)?
  - Is the test in part (b) a uniformly most powerful critical region for testing  $H_0 : p = 0.9$  when the alternative hypothesis is  $H_1 : p < 0.9$ ?
- 6.5.3 Let  $X_1, \dots, X_n$  be a random sample from the normal distribution  $N(\mu, 36)$ .
- Show that a uniformly most powerful critical region for testing  $H_0 : \mu = 50$  against  $H_1 : \mu < 50$  is given by  $C_2 = \{(x_1, \dots, x_n) : \bar{x} \leq c\}$ .
  - With this result and the example discussed in class argue that a uniformly most powerful test for testing  $H_0 : \mu = 50$  against  $H_1 : \mu \neq 50$  does not exist.