

Chapter 21: Saving Models

For All Practical
Purposes



Mathematical Literacy in
Today's World, 9th ed.

Section 21.1 Arithmetic Growth and Simple Interest

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Arithmetic Growth and Simple Interest

Principal – The initial balance of the savings account.

Interest – Money earned on a savings account or a loan.

Example: The amount of interest on 10% of the principal of \$1000 is
 $10\% \times \$1000 = 0.10 \times \$1000 = \$100$

Simple Interest

- ❑ The method of paying interest only on the initial balance in an account, not on any accrued interest.

Example: The following shows the simple interest of a savings account with a principal of \$1000 and a 10% interest rate:

- ❑ End of first year, you receive \$100 interest.
- ❑ The account total at the start of the second year is \$1100.
- ❑ End of second year, you receive again only \$100, which is the interest from the original balance of \$1000.
- ❑ Account total at the beginning of the third year is \$1200.
- ❑ At the end of each year you receive just \$100 in interest.

Arithmetic Growth and Simple Interest

Bonds

- ❑ An obligation to repay a specified amount of money at the end of a fixed term, with simple interest usually paid annually.

- ❑ Interest Rate Formula: $I = Prt$

- ❑ The total amount accumulated:

$$A = P(1 + rt) = P + Prt = P + I$$

Example: Say you deposited \$10,000. What would be the total amount accumulated in 10 years at 4.0% simple interest?

Answer:

$P = \$10,000$, $r = 4.0\% = 0.04$, and $t = 10$ yrs.

Interest, $I = Prt = (10,000)(0.04)(10) = \4000

Total $A = P(1 + rt) = 10,000(1 + (0.04)(10))$
 $= 10,000(1.40) = \$14,000$

Interest Rate Formula –

$$I = Prt$$

Where:

$I =$ Simple interest earned

$P =$ Principal amount

$r =$ Annual rate of interest

$t =$ Time in years

Total Amount Accumulated

$$A = P(1 + rt)$$

Arithmetic Growth – (linear growth) $A = P(1 + rt)$

Arithmetic Growth

Simple interest: Interest is paid per year on the original balance only, no matter how much interest has accumulated.

Example: \$1000 is deposited at simple interest of 10%. What will the total principal be after

- Solution:**
- | | |
|-------------|--|
| a) 1 year | a) End of 1 st year: $\$1000 + 0.10(\$1000)$ |
| b) 2 years | $= \$1000 + \100 |
| c) 3 years | $= \$1100$ |
| d) 20 years | b) End of 2 nd year: $\$1000 + 2(\$100) = \$1200$ |
| e) n years | c) End of 3 rd year: $\$1000 + 3(\$100) = \$1300$ |
| | d) End of 20 years: $\$1000 + 20(\$100) = \$3000$ |
| | e) End of n years: $\$1000 + n(\$100)$ |

Old Exam Question

If you deposit \$2000 at 7% simple interest, what is the balance after 2 years?

A) \$2280.00

B) \$2289.80 $\$2000 + 2 \times (\$2000 \times 0.07) = \$2280.00$

C) \$2295.05

D) \$2300.52