

# Chapter 16: Identification Numbers

For All Practical  
Purposes



Mathematical Literacy in  
Today's World, 9th ed.

## Section 16.1 Check Digits (U.S. Postal Service Money Order)

James Baglama  
Department of Mathematics  
University of Rhode Island



## Chapter 16: Identification Numbers

### ■ Identification Numbers

- ❑ Modern identification numbers serve at least two functions:
  1. The number should unambiguously identify the person or thing with which it is associated .
  2. The number should have a “self-checking” aspect.



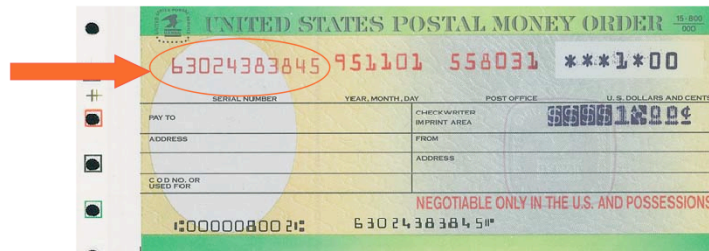
### ■ Code

- ❑ A group of symbols that represent information.
- ❑ Codes have been invented for storing, securing, and transmitting information.
- ❑ Examples: Hieroglyphics, the Greek alphabet, Roman numerals, Morse code, and the “genetic code” used to describe DNA

## Check Digits

- Check Digit
  - A digit included in an identification number for the purpose of error detection.
    - Mathematical calculations or schemes are used on the digits of the identification number to assign the check digit.
    - Computers use the check digit to help detect typing errors during data entry to prevent and detect fraud and to find other errors.

- ❑ **U.S. Postal Service money order** with identification number 6302438384 and check digit 5.



- ❑ The check digit in this case is the *calculated remainder after dividing the sum of the first ten digits by 9*.

## Example: Postal Service Money Order



The check digit = the remainder obtained when the sum of the first 10 digits of the number is divided by 9

$$6+3+0+2+4+3+8+3+8+4=41$$

The remainder when 41 is divided by 9 is 5.

## Remarks on remainder

Example: 418 divide by 7

---

If you plug this problem into a calculator, you'll get 59.7143.

Doing it using long division, you can work it out this way:

$$\begin{array}{r} 59 \text{ R } 5 \\ 7 \overline{) 418} \\ \underline{-35} \phantom{0} \\ 68 \\ \underline{-63} \\ 5 \end{array}$$

The **R** stands for 'remainder.' That is, the number to the right of the **R** is the remainder of this division.

**Example:**

Suppose a U. S. Postal Service money order is numbered 632930421#, where the last digit is obliterated. What is the missing digit?

**Example:** Postal Service Money Order



The check digit = the remainder obtained when the sum of the first 10 digits of the number is divided by 9

$$6+3+0+2+4+3+8+3+8+4=41$$

The remainder when 41 is divided by 9 is 5.

**Example:**

Suppose a U. S. Postal Service money order is numbered 632930421#, where the last digit is obliterated. What is the missing digit?

**Solution:**

$$6 + 3 + 2 + 9 + 3 + 0 + 4 + 2 + 1 = 30$$

When 30 is divided by 9, the remainder is 3. The 11<sup>th</sup> digit (Check Digit) is then 3.

<http://www.math.upenn.edu/~deturck/m170/wk1examples/calc.html>