

# Chapter 16: Identification Numbers

For All Practical  
Purposes



Mathematical Literacy in  
Today's World, 9th ed.

## Section 16.1 Check Digits (Bank Checks and Codabar )

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## Check Digits

- Check Digit
  - A digit included in an identification number for the purpose of error detection.
    - Mathematical calculations or schemes are used on the digits of the identification number to assign the check digit.
    - Computers use the check digit to help detect typing errors during data entry to prevent and detect fraud and to find other errors.

■ Bank Identification Number

□ Here is what the string of numbers at the bottom of a check mean:

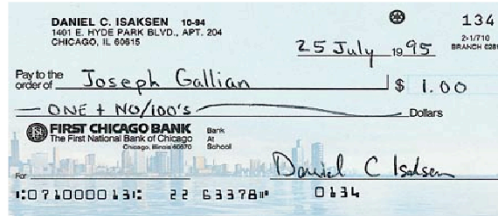
**0710** Bank's Federal Reserve District, office, and state or special collection arrangement

**0001** Bank's ID number

**3** Check digit (error detection)

**22 633 78** Checking account number

**0134** Customer's check number



The First Chicago Bank has the routing number 07100001 3 on the bottom of all its checks. Scheme uses the multipliers 7 - 3 - 9 (without the check digit) on the first 8 digits.  
 $7(\text{digit } 1) + 3(\text{digit } 2) + 9(\text{digit } 3) + 7(\text{digit } 4) + 3(\text{digit } 5) + 9(\text{digit } 6) + 7(\text{digit } 7) + 3(\text{digit } 8)$

The check digit 3 is the last digit of the sum:

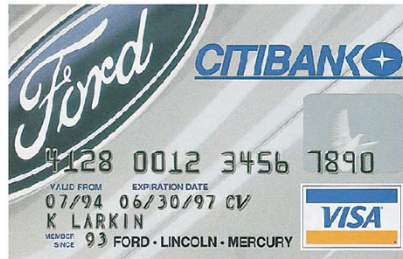
$$(7) \cdot 0 + (3) \cdot 7 + (9) \cdot 1 + (7) \cdot 0 + (3) \cdot 0 + (9) \cdot 0 + (7) \cdot 0 + (3) \cdot 1 = 33.$$

↑  
 \_\_\_\_\_  
 Check Digit

3

■ Codabar

- ❑ An error-detection method used by all major credit-card companies, many libraries, etc.
- ❑ After the bank issues a card number, it adds an extra digit for error detection created by certain math calculations using a check digit scheme. This makes it difficult to create phony credit cards!

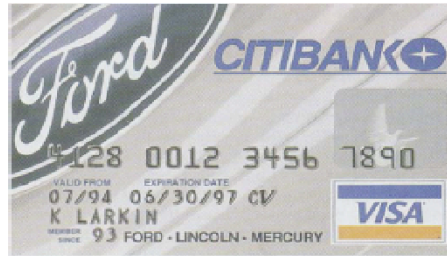


One of the most efficient error-detection  
methods: **Codabar**

The Codabar system is a variation of UPC using a similar sum with weights 2 (odd positions) and 1 (even positions). To this sum, add the number of digits in odd positions that exceed 4; The resulting number must end in 0 to be a valid Codabar code.

$$\begin{aligned} &(4+2+0+1+3+5+7+9)*2 \\ &+(1+8+0+2+4+6+8)*1 \\ &+3=94 \end{aligned}$$

which does not end in 0, so  
This credit card is not valid.



Position number: 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16  
Card #: 4 1 2 8-0 0 1 2-3 4 5 6 -7 8 9 0

**Example:**

Determine the check digit that should be appended to the Codabar number 3125-8001-6535-003#.

**Example:**

Determine the check digit that should be appended to the Codabar number 312580016535003.

**Solution:**

Position number: 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16

Card #: 3 1 2 5 8 0 0 1 6 5 3 5 0 0 3 ?

Odd Positions:  $2*(3 + 2 + 8 + 0 + 6 + 3 + 0 + 3) = 50$

Even Positions:  $(1 + 5 + 0 + 1 + 5 + 5 + 0 + ?) = 17$

Add even and values to get 67. Now add in the number of values in the odd positions that exceed four = 2. ( $67 + 2 = 69$ ). The calculated sum is 69. When 1 is added to 69, the result is 70, which ends in zero. The check digit is then 1.

Try the example without reading the answer first.