

## Maple Project I

### Polar Plots

To plot in maple the **parametric equations**

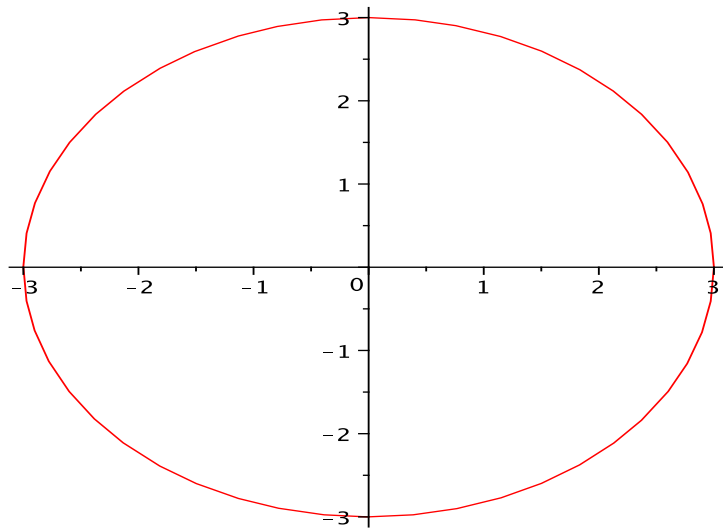
$$x=f(t), y=g(t), \text{ with } t \text{ in } [a,b]$$

We type the command:

```
plot([f(t), g(t), t=a..b]);
```

For example, to plot a circle of radius 3 centered at the origin, we type

```
> plot([3*cos(t), 3*sin(t), t=0..2*Pi], scaling=constrained);
```



To plot the polar equation

$$r=r(t), t \text{ in } [\alpha, \beta]$$

where  $\alpha$  and  $\beta$  are certain angles, we need to convert the given equation from **polar coordinates** to **rectangular coordinates** using the equations:

$$x = r \cos ( t ) , y = r \sin ( t )$$

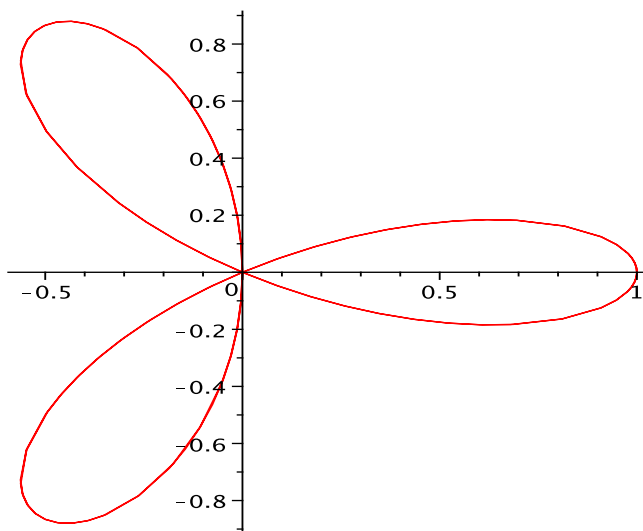
**Example:**

Plot the polar equation

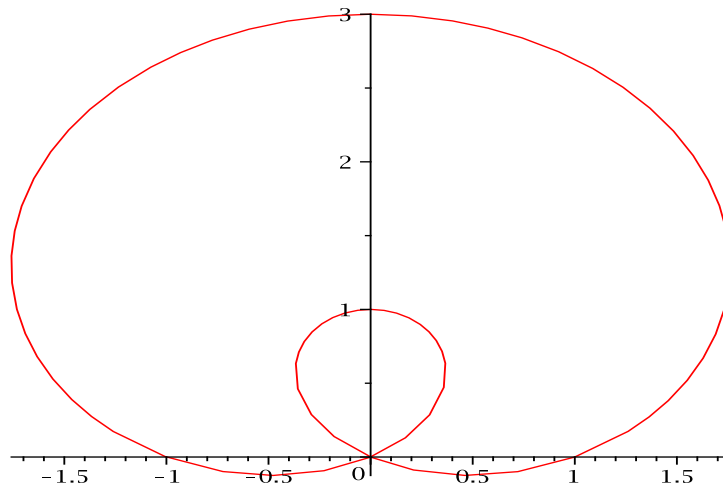
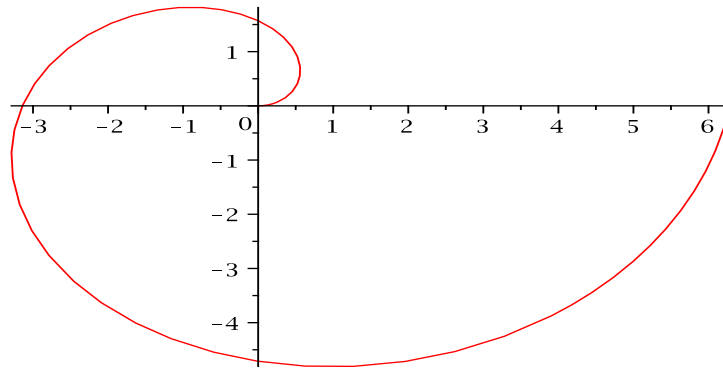
$$r = \cos(3t), \text{ where } t \text{ in } [0, 2\pi]$$

In maple format:

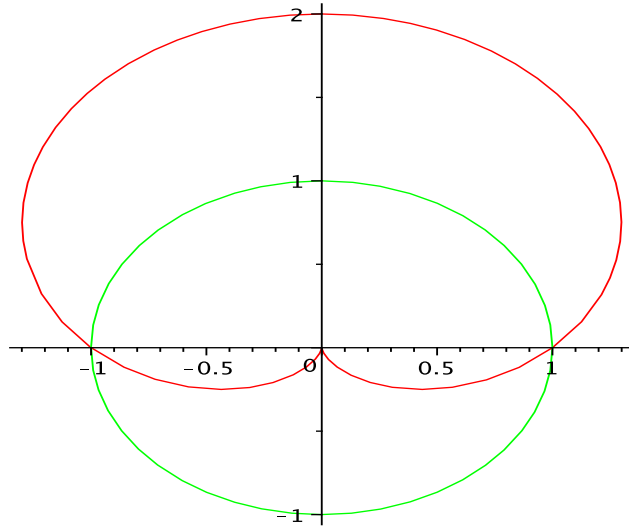
```
> r:=cos(3*t): plot([r*cos(t), r*sin(t), t=0..2*Pi], scaling=constrained);
```



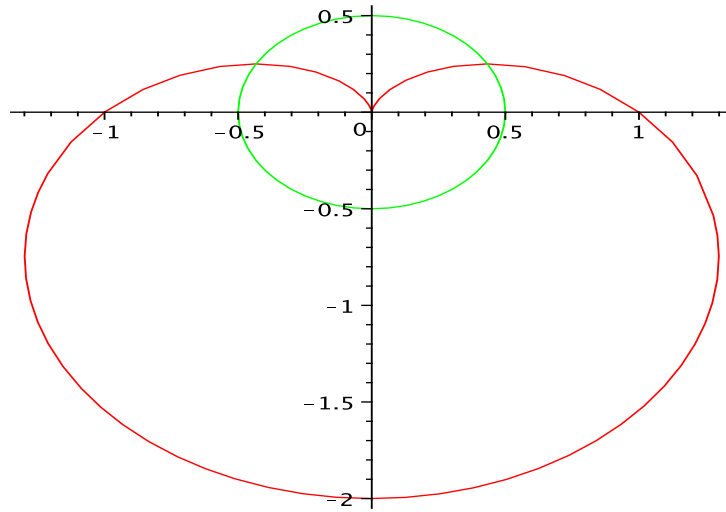
```
> r:=t: plot([r*cos(t), r*sin(t), t=0..2*Pi], scaling=constrained);
```



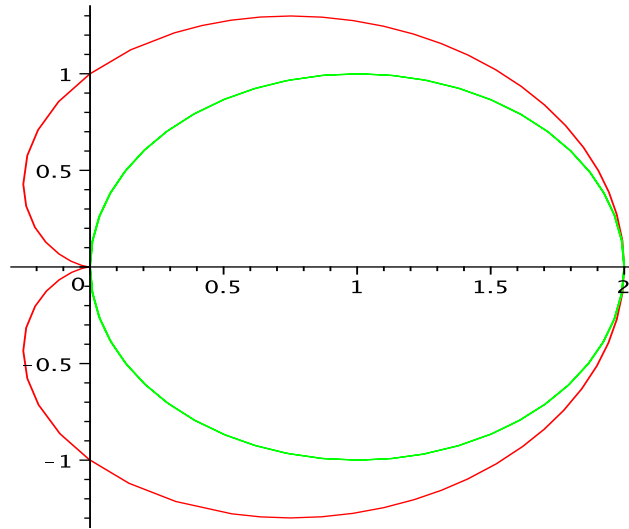
```
> s:=1: r:=1+sin(t): plot({[s*cos(t), s*sin(t), t=0..2*Pi], [r*cos(t),
r*sin(t), t=0..2*Pi]}, scaling=constrained);
```



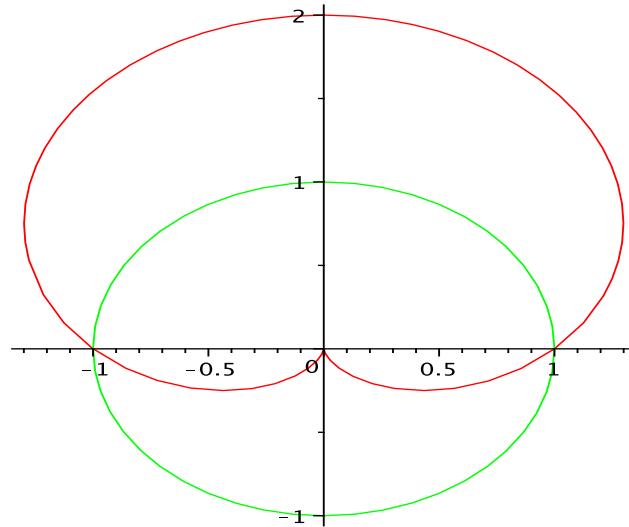
```
> s:=1./2: r:=1-sin(t): plot({[s*cos(t), s*sin(t), t=0..2*Pi],
[r*cos(t), r*sin(t), t=0..2*Pi]}, scaling=constrained);
```



```
> s:=2*cos(t): r:=1+cos(t): plot({[s*cos(t), s*sin(t), t=0..2*Pi],
[r*cos(t), r*sin(t), t=0..2*Pi]}, scaling=constrained);
```



```
> r:=1+sin(t): s:=1: plot([r*cos(t), r*sin(t), t=0..2*Pi], [s*cos(t),
s*sin(t), t=0..2*Pi]), scaling=constrained);
```



**Homework:**

1). Using constrained scaling, plot the ellipse

$$x = 3 \cos ( t ) \text{ and } y = \sin ( t )$$

2). Curves of the form:

equation1:  $r = a \sin ( n * t )$  or equation2:  $r = a \cos ( n * t )$  for " $a \neq 0$ " and " $n \neq 0$ " are called Roses. For " $a=2$ " and " $n=3$ " draw the graphs of equations 1 and 2, compare them and report your observations. Repeat this step for " $a=2$ " and " $n=4$ ".

3). Curves of the form:

equation1:  $r=a+b \sin (t)$  orequation2:  $r= a+b \cos(t)$   
are called "limacons". Repeat the steps in problem(2) for this problem with  
"a=2 and b=3" , "a=2 and b=-3" and  
"a=2 and b=1".

4).Graph each of the following equations.

a). $r = \sin ( 2t )$

b). $r= 2\cos ( t ) + 1$

c). $r^2= \cos ( 2 t )$  5).Find the intersection points of the parabolas

$$r= 1/(1 - \cos ( t ) ) \text{ and } r= 3/(1 + \cos ( t ) )$$

Hint: To get a better display of the graphs restrict your plot to the window [-5, 5]x[-5,5]